## Errata and Updates for ASM Exam SRM Study Manual (Third Edition)

## (Last updated 6/9/2023) sorted by page

Page 106 The second edition of An Introduction to Statistical Learning modified their formulas for AIC and BIC of a linear regression by removing  $\sigma^2$ from the denominators. Thus on the manual's page 106, formulas (7.4) and (7.5) should be changed to

$$AIC = \frac{1}{n} (RSS + 2d\hat{\sigma}^2)$$
(7.4)

$$BIC = \frac{1}{n} \left( RSS + (\ln n) d\hat{\sigma}^2 \right)$$
(7.5)

Pages 113 and 120 Exercises 7.17 and 7.18 require modification.

7.17 For a linear regression model with 100 observations, you are given:

- The model has 10 variables and an intercept.
- The residual sum of squares is 64.8.
- The estimated variance of the residual term is 5.5.

Calculate AIC and BIC using the formulas in James et al. Solution

AIC = 
$$\frac{1}{100} (64.8 + 2(10)(5.5)) = 1.748$$
  
BIC =  $\frac{1}{100} (64.8 + (\ln 100)(10)(5.5)) = 3.181$ 

7.18 A linear regression model has n observations and 8 predictors. You are testing a model having a subset of the 8 predictors. The subset has 4 predictors.

You are given:

- Both models have intercepts.
- The training RSS of the original model is 82.8.

- The training RSS of the subset model is 116.2.
- The variance of the residuals is estimated using the original model.
- AIC and BIC of the subset model are calculated using the formulas in James et al.
- The AIC of the subset model is 105.2458.

Calculate the BIC of the subset model.

## Solution

$$\hat{\sigma}^2 = \frac{82.8}{n-9}$$
AIC =  $n - 9n (116.2 + (2)(4)(82.8)n - 9)$ 
 $105.2458 = \frac{116.2(n-9) + 8(82.8)}{n}$ 
 $105.2458n = 116.2n - 383.4$ 
 $n = \frac{383.4}{10.9542} = 35$ 
BIC =  $2635 \left( 116.2 + \frac{(\ln 35)(4)(82.8)}{26} \right) = 110.9638$ 

- Page 262 In Exercise 15.10, in the three bullets, the models should be numbered as Model I, Model II, and Model III respectively.
- Page 274 On the line above the first displayed expression, change "mean square error" to RSS. One line and three lines below the displayed expression, change MSE to RSS.
- Page 295 Replace the solution to exercise 16.5 with the following:

Splits I and III don't split at all; all observations go into  $R_2$ . Split II puts (4,1) into  $R_2$  and everything else into  $R_1$ . There is no error for (4,1), whereas the error of the other 5 is the square difference from the mean, or the population (division by 5) variance times 5, which is 0.548. Split IV puts (1,0) into  $R_1$  and everything else into  $R_2$ . Once again, we can compute the RSS as the variance in  $R_2$ , or 0.2824, times 5, or 1.412. Split V puts two observations, (3,2) and (2,2), into  $R_2$  and the others into  $R_1$ . The variance of the observations in  $R_1$  is 0.451875 so the sum of squares is 4(0.451875) = 1.8075. The RSS for  $R_2$  is  $(1.5-1.75)^2 + (2-1.75)^2 = 0.125$ . The total RSS for this split is 1.8075 + 0.125 = 1.9325. Split II minimizes the RSS. (B)

Page 295 In the solution to Exercise 16.8, on the fifth line, change "86 + 82 + 81 + 4(9) = 286 to 82 + 81 + 11 + 86 + 4(9) = 296.